

June 23th, 2008

Assignment C5

(classroom assignment)

Problem: Consider the integral equation

$$u(x) = \mu \int_0^\pi (\cos^2(x) \cos(2t) + \cos^3(t) \cos(3x)) u(t) dt.$$

Calculate the characteristic values and the corresponding eigenfunctions of this equation.

Hint: Observe

$$\begin{aligned} \int \cos^3(x) \cdot \cos(3x) dx &= \frac{1}{8}x + \frac{3}{16}\sin(2x) + \frac{3}{32}\sin(4x) + \frac{1}{48}\sin(6x) + C, \\ \int \cos^2(x) \cdot \cos(2x) dx &= \frac{1}{4}x + \frac{1}{4}\sin(2x) + \frac{1}{16}\sin(4x) + C. \end{aligned}$$